

You may wish to recall the following facts for  $f \in \Lambda^0(\mathbb{R}^n)$ ,  $\alpha, \gamma \in \Lambda^p(\mathbb{R}^n)$  and  $\beta \in \Lambda^q(\mathbb{R}^n)$ :

$$\begin{aligned}
 *1 &= \omega \\
 ** &= (-1)^{p(n-p)+s} \\
 df &= \frac{\partial f}{\partial x^i} dx^i \\
 d^2 &= 0 \\
 \beta \wedge \alpha &= (-1)^{pq} \alpha \wedge \beta \\
 \alpha \wedge *\gamma &= g(\alpha, \gamma) \omega \\
 d(f d\alpha) &= df \wedge d\alpha \\
 d(\alpha \wedge \beta) &= d\alpha \wedge \beta + (-1)^p \alpha \wedge d\beta \\
 d\vec{r} &= \sigma^i \hat{e}_i \\
 ds^2 &= d\vec{r} \cdot d\vec{r}
 \end{aligned}$$

You may wish to use the following relationships in (Euclidean)  $\mathbb{R}^3$ :

$$\begin{aligned}
 \vec{F} \cdot d\vec{r} &= F \\
 \vec{F} \cdot \vec{G} &= *(F \wedge *G) \\
 (\vec{F} \times \vec{G}) \cdot d\vec{r} &= *(F \wedge G) \\
 \vec{\nabla} f \cdot d\vec{r} &= df = \nabla f \\
 (\vec{\nabla} \times \vec{F}) \cdot d\vec{r} &= *dF = \nabla \times F \\
 \vec{\nabla} \cdot \vec{F} &= *d*F = \nabla \cdot F \\
 \Delta f &= \vec{\nabla} \cdot \vec{\nabla} f = *d*df = \nabla \cdot \nabla f \\
 h_u &= \left| \frac{\partial \vec{r}}{\partial u} \right|
 \end{aligned}$$