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**USEFUL EQUATIONS:** ( $f \in \Lambda^0$ ,  $\alpha, \gamma \in \Lambda^p$ ,  $\beta \in \Lambda^q$ )

$$\begin{aligned}
\beta \wedge \alpha &= (-1)^{pq} \alpha \wedge \beta & d(f d\alpha) &= df \wedge d\alpha \\
d^2\alpha &= 0 & d(\alpha \wedge \beta) &= d\alpha \wedge \beta + (-1)^p \alpha \wedge d\beta \\
\alpha \wedge *\gamma &= g(\alpha, \gamma) \omega & ** &= (-1)^{p(n-p)+s} \\
d\vec{e}_j &= \omega^i_j \vec{e}_i & \omega_{ij} &= \vec{e}_i \cdot d\vec{e}_j & \omega_{ij} + \omega_{ji} &= 0 \\
d\vec{r} &= \sigma^i \vec{e}_i & d^2\vec{r} &= \vec{0} & d^2\vec{e}_j &= \Omega^i_j \vec{e}_i \\
d\sigma^i + \omega^i_j \wedge \sigma^j &= 0 & \omega^i_j &= \Gamma^i_{jk} \sigma^k \\
d\omega^i_j + \omega^i_k \wedge \omega^k_j &= \Omega^i_j = \frac{1}{2} R^i_{jkl} \sigma^k \wedge \sigma^l \\
\Omega^i_j \wedge \sigma^j &= 0 & d\Omega^i_j + \omega^i_k \wedge \Omega^k_j - \Omega^i_k \wedge \omega^k_j &= 0 \\
S = -(\Gamma^3_{ij}) & \det S = K & \Omega^1_2 &= d\omega^1_2 = K \sigma^1 \wedge \sigma^2 \\
\kappa_g ds = d\hat{\mathbf{T}} \cdot \hat{\mathbf{N}} &= d\alpha - \omega^1_2 & \int_S K \omega + \oint_{\partial S} \kappa_g ds &= 2\pi \\
\int_R d\alpha &= \int_{\partial R} \alpha & \int_\Sigma K \omega &= 2\pi\chi(\Sigma) = 2\pi(v - e + f) \\
2 \sin^2 \theta &= 1 - \cos 2\theta & \frac{d}{d\theta} \ln \tan \frac{\theta}{2} &= \frac{1}{\sin \theta} \\
\cosh^2 \psi - \sinh^2 \psi &= 1 & 2 \cosh \psi &= e^\psi + e^{-\psi} & 2 \sinh \psi &= e^\psi - e^{-\psi}
\end{aligned}$$

You may wish to use the following relationships in (Euclidean)  $\mathbb{R}^3$ :

$$\begin{aligned}
\vec{\mathbf{F}} \cdot d\vec{\mathbf{r}} &= F \\
\vec{\nabla} f \cdot d\vec{\mathbf{r}} &= df \\
(\vec{\nabla} \times \vec{\mathbf{F}}) \cdot d\vec{\mathbf{r}} &= *dF \\
\vec{\nabla} \cdot \vec{\mathbf{F}} &= *d*F \\
\Delta f &= \vec{\nabla} \cdot \vec{\nabla} f = *d*df
\end{aligned}$$


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