

Review

\wedge

stacks
vector calculus

$*$

$d\vec{r}$

d

orthonormal bases

g

signature

$$g(\alpha, \beta) = *(\alpha \wedge * \beta) (-1)^s$$

$$\alpha \wedge * \beta = g(\alpha, \beta) \omega$$

$$*1 = \omega$$

$$*\omega = (-1)^s$$

$$**\alpha = (-1)^{s+p(n-p)} \alpha \quad [\alpha \in \wedge^p(\mathbb{R}^n)]$$

$$d\vec{r} = \nabla^i \hat{e}_i$$

orthonormal

$$\beta \wedge \alpha = (-1)^{pq} \alpha \wedge \beta \quad [\alpha \in \wedge^p, \beta \in \wedge^q]$$

$$d(\alpha \wedge \beta) = d\alpha \wedge \beta + (-1)^p \alpha \wedge d\beta$$

"derivation" $d^2 = 0$

$$\alpha(\vec{v}) = \alpha_i v^i \quad \begin{array}{l} d = \alpha_i \sigma^i \\ \vec{v} = v^i \hat{e}_i \end{array}$$

$$df(\vec{v}) = \vec{v}(f) = v^i \frac{\partial f}{\partial x^i} \leftarrow df$$