Name \_

MTH 434/534

MIDTERM

Work on the paper provided, turn in this page as well and put your name on each page. Feel free to ask questions during the exam — I will answer any I feel are appropriate. Show your work! It is to your advantage to turn in all your scratch work (clearly labeled!). In particular, it is to your advantage **not** to erase anything.

You should attempt every problem. If you are unable to complete a calculation, set it up and give a clear description of what you would have done for possible partial credit. Do not waste time on unnecessary simplifications, which will not substantially improve your grade.

You may wish to recall the following facts for  $f \in \bigwedge^0(\mathbb{R}^n)$ ,  $\alpha, \gamma \in \bigwedge^p(\mathbb{R}^n)$  and  $\beta \in \bigwedge^q(\mathbb{R}^n)$ :

$$** = (-1)^{p(n-p)+s}$$
$$df = \frac{\partial f}{\partial x^i} dx^i$$
$$d^2 = 0$$
$$\beta \wedge \alpha = (-1)^{pq} \alpha \wedge \beta$$
$$\alpha \wedge *\gamma = g(\alpha, \gamma) \omega$$
$$d(f \, d\alpha) = df \wedge d\alpha$$
$$d(\alpha \wedge \beta) = d\alpha \wedge \beta + (-1)^p \alpha \wedge d\beta$$

You may wish to use the following relationships in (Euclidean)  $\mathbb{R}^3$ :

$$\vec{F} \cdot d\vec{r} = F$$
$$\vec{F} \cdot \vec{G} = *(F \wedge *G)$$
$$(\vec{F} \times \vec{G}) \cdot d\vec{r} = *(F \wedge G)$$
$$\vec{\nabla} f \cdot d\vec{r} = df = \nabla f$$
$$(\vec{\nabla} \times \vec{F}) \cdot d\vec{r} = *dF = \nabla \times F$$
$$\vec{\nabla} \cdot \vec{F} = *d*F = \nabla \cdot F$$
$$\Delta f = \vec{\nabla} \cdot \vec{\nabla} f = *d*df = \nabla \cdot \nabla f$$
$$h_u = \left| \frac{\partial \vec{r}}{\partial u} \right|$$