

You may wish to recall the following facts:

$$\begin{aligned} ** &= (-1)^{p(n-p)+s} \\ d^2 &= 0 \\ \beta \wedge \alpha &= (-1)^{pq} \alpha \wedge \beta \\ \alpha \wedge *\gamma &= g(\alpha, \gamma) \omega \\ d(\alpha \wedge \beta) &= d\alpha \wedge \beta + (-1)^p \alpha \wedge d\beta \end{aligned}$$

You may wish to use the following relationships in (Euclidean) \mathbb{R}^3 :

$$\begin{aligned} \vec{F} \cdot d\vec{r} &= F \\ \vec{\nabla} f \cdot d\vec{r} &= df \\ (\vec{\nabla} \times \vec{F}) \cdot d\vec{r} &= *dF \\ \vec{\nabla} \cdot \vec{F} &= *d*F \\ \Delta f &= \vec{\nabla} \cdot \vec{\nabla} f = *d*df \end{aligned}$$