

**SAMPLE EXAM QUESTIONS**  
**MTH 420**

1. Suppose  $d\alpha = \beta$ . Find  $d(\alpha \wedge \beta)$ .
2. Consider 2-dimensional Minkowski space, i.e.  $\mathbb{R}^2$  with coordinates  $(t, x)$ , inner product
$$g(dt, dt) = -1 \quad g(dt, dx) = 0 \quad g(dx, dx) = 1$$
and orientation  $\omega = dx \wedge dt$ . Find the Laplacian  $\Delta f = *d*df$  of a function  $f$ .
3. Calculate the curl  $\nabla \times F = *dF$  of a vector field  $F$  in (Euclidean)  $\mathbb{R}^3$  using the **orthonormal** spherical basis  $\{dr, r d\theta, r \sin \theta d\phi\}$ .