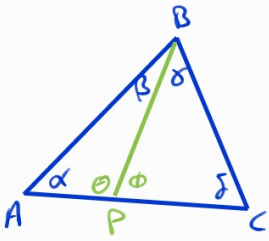


Recall: angle sum for any hyperbolic triangle is  $< 180^\circ$  ( $S < 180^\circ$ )

Def: The defect  $D$  of a (hyperbolic) triangle is:

$$D = 180 - S$$

- swBQ:
- Draw triangle
  - Label angles
  - Write expression for D
  - Divide into 2 triangles
  - Repeat above for each
  - Add defects

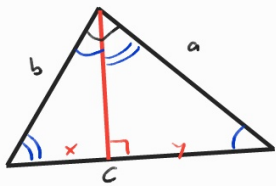


$$\begin{aligned}
 D(\triangle ABP) &= 180 - (\alpha + \beta + \theta) \\
 + D(\triangle BCP) &= 180 - (\delta + \gamma + \phi) \\
 \hline
 &= 360 - (\alpha + \beta + \theta + \delta + \gamma + \phi) \\
 &= 180 - (\alpha + \beta + \gamma) \\
 &= D(\triangle ABC)
 \end{aligned}$$

$\therefore$  Thm: Defects add!

Corollary:  $D(\triangle ABC) > D(\triangle ABP)$   
 (since  $S < 180 \Rightarrow D > 0$ )

Pythagorean Theorem  
(Euclidean Geometry)



$$\frac{x}{b} = \frac{b}{c} \Rightarrow b^2 = xc$$
$$\frac{y}{a} = \frac{a}{c} \Rightarrow a^2 = yc$$
$$\Rightarrow a^2 + b^2 = (x+y)c = c^2$$

Pythagorean Theorem (4.4.8)

uses: AAA similarity ← uses  $A = \frac{1}{2}bh$ , which is SMSG 20  
 $\Sigma$  angles =  $\pi$  ← parallel postulate

AAA Congruence  
(hyperbolic geometry)

Suppose not. Then no sides match  
(else ASA)

Thus, 2 sides must be larger:

