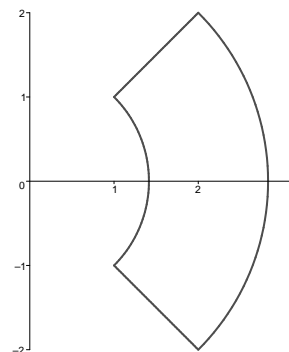
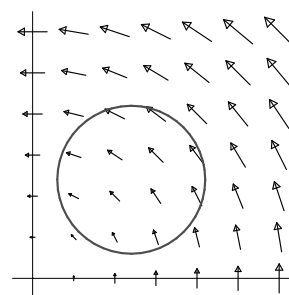


1. For each of the problems below, say whether you expect the given vector field to have positive, negative, or zero circulation *counterclockwise* around the closed curve C in the figure shown at the right. Two of the segments of C are circular arcs centered at the origin; the other two are radial line segments. You may find it helpful to sketch the vector field.



- (a) $\vec{G} = x \hat{i} + y \hat{j}$
 (b) $\vec{H} = y \hat{i} - x \hat{j}$

2. Consider the vector field \vec{F} shown at the right, and the loop C , which is to be traversed in the *counterclockwise* direction.



- (a) Is $\oint_C \vec{F} \cdot d\vec{r}$ positive, negative, or zero?

- (b) Which of the following formulas best fits \vec{F} ?

$$\vec{F}_1 = \frac{x}{x^2 + y^2} \hat{i} + \frac{y}{x^2 + y^2} \hat{j}$$

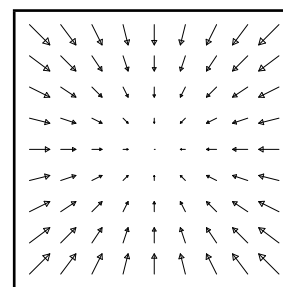
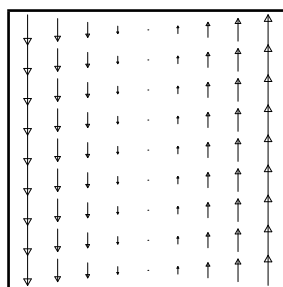
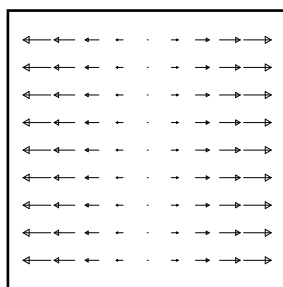
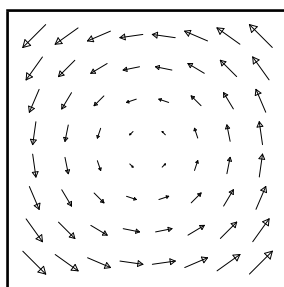
$$\vec{F}_2 = -y \hat{i} + x \hat{j}$$

$$\vec{F}_3 = \frac{-y}{(x^2 + y^2)^2} \hat{i} + \frac{x}{(x^2 + y^2)^2} \hat{j}$$

3.

- (a) For each vector field \vec{F} shown below, sketch a curve for which the integral $\int_C \vec{F} \cdot d\vec{r}$ is positive.

- (b) For which of these vector fields is it possible to choose your curve to be closed?



EXTRA CREDIT:

From your answer to part (a) of problem 2, can you determine whether or not $\vec{F} = \vec{\nabla} f$ for some function f ?