## MTH 255

## HW #3

Consider a valley whose height h in meters is given by  $h = \frac{x^2}{10} + \frac{y^2}{10}$ , with x and y (and 10!) in meters. Suppose you are hiking through this valley on a trail given by 1.

$$x = 3t \qquad y = 2t^2$$

with t in seconds (and where "3" and "2" have appropriate units).

- (a) How fast are you climbing (rate of change of h) per meter along the trail when t = 1? You may find it helpful to recall that  $ds = |d\vec{r}|$ .
- (b) How fast are you climbing *per second* when t = 1.

2.

- (a) For each vector field  $\vec{F}$  shown below, sketch a curve for which the integral  $\int \vec{F} \cdot d\vec{r}$  is positive.
- (b) For which of these vector fields is it possible to choose your curve to be closed?



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