



**Abstract**

The PER community has developed and studied many tools designed to increase interactive engagement in physics classrooms. We present a narrative of using Small White Board Questions (SWBQs) to achieve active engagement. The instructor used a sequence of SWBQs to help the students induce the full Hamiltonian for the hydrogen atom by starting from their knowledge of the Hamiltonian for a 1D particle-in-a-box. We highlight two affordances of this type of sequence: allowing students to build their understanding of a complex system starting from a simple question and providing for increased instructor responsiveness to students' ideas and questions.

**SWBQ RITUALS**

**Narrative**

Narratives are a form of story-telling. A narrative reports interesting incidents that happened during a class period: what the students and instructor said and did during this time interval and commentary based upon insights articulated by the instructor, and perhaps colleagues, while watching a video of the interaction.



**The Schrödinger Equation**

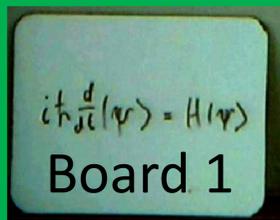
**Goals:** To ensure that students understand the importance of the Schrödinger equation and to give them a chance to wrestle with the details and with the differences between bra-ket and wave function notation.

**Prompt:** "Write down the Schrödinger equation."

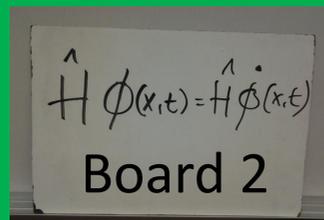
**Observing:**



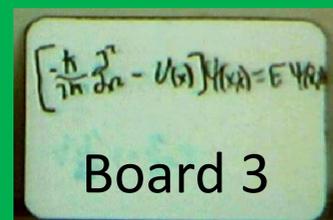
**Choosing:**



Board 1



Board 2



Board 3

Three boards that the instructor chose that highlight ideas in the room

**Discussing Answers :**

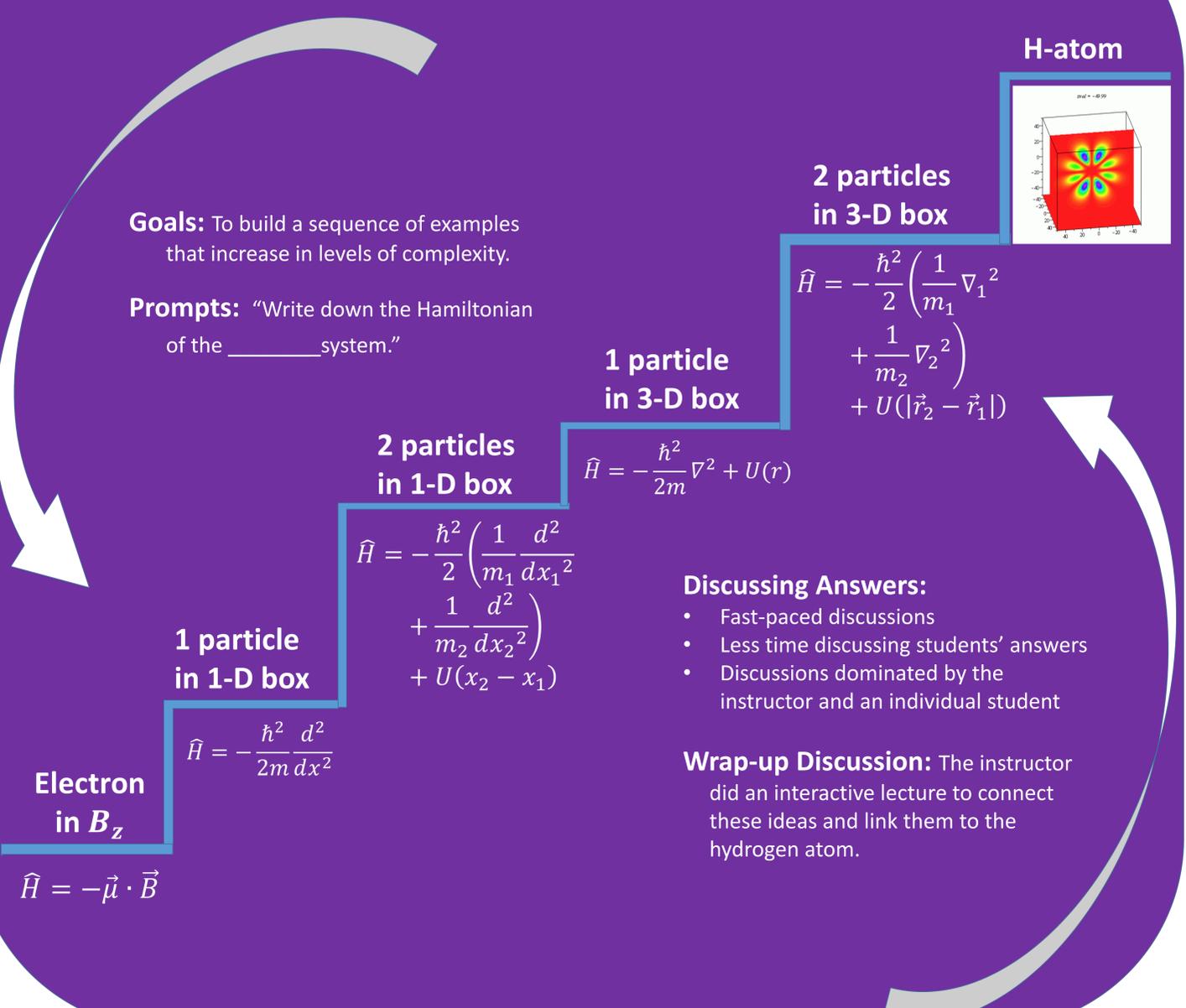
- Slow-paced discussion
- More time spent discussing students' answers
- Discussions happening all around the room (student to student and students to the instructor)

**Wrap-up Discussion:** The instructor connected these discussions to the next portion of the class which builds up to the complexity of the Hamiltonian of the hydrogen atom.

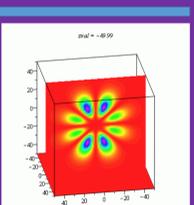
**Building Up Complexity**

**Goals:** To build a sequence of examples that increase in levels of complexity.

**Prompts:** "Write down the Hamiltonian of the \_\_\_\_\_ system."



**H-atom**



**2 particles in 3-D box**

$$\hat{H} = -\frac{\hbar^2}{2} \left( \frac{1}{m_1} \nabla_1^2 + \frac{1}{m_2} \nabla_2^2 \right) + U(|\vec{r}_2 - \vec{r}_1|)$$

**1 particle in 3-D box**

$$\hat{H} = -\frac{\hbar^2}{2m} \nabla^2 + U(r)$$

**2 particles in 1-D box**

$$\hat{H} = -\frac{\hbar^2}{2} \left( \frac{1}{m_1} \frac{d^2}{dx_1^2} + \frac{1}{m_2} \frac{d^2}{dx_2^2} \right) + U(x_2 - x_1)$$

**1 particle in 1-D box**

$$\hat{H} = -\frac{\hbar^2}{2m} \frac{d^2}{dx^2}$$

**Electron in  $B_z$**

$$\hat{H} = -\vec{\mu} \cdot \vec{B}$$

**Discussing Answers:**

- Fast-paced discussions
- Less time discussing students' answers
- Discussions dominated by the instructor and an individual student

**Wrap-up Discussion:** The instructor did an interactive lecture to connect these ideas and link them to the hydrogen atom.