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Circuits with Light at Nanoscales: Optical Nanocircuits Inspired by Metamaterials

Nader Engheta

A form of optical circuitry is overviewed in which a tapestry of subwavelength nanometer-scale metamaterial structures and nanoparticles may provide a mechanism for tailoring, patterning, and manipulating local optical electric fields and electric displacement vectors in a subwavelength domain, leading to the possibility of optical information processing at the nanometer scale. By exploiting the optical properties of metamaterials, these nanoparticles may play the role of “lumped” nanocircuit elements such as nanoinductors, nanocapacitors, and nanoresistors, analogous to microelectronics. I show that this concept of metamaterial-inspired nanoelectronics (“metatronics”) can bring the tools and mathematical machinery of the circuit theory into optics, may link the fields of optics, electronics, plasmonics, and metamaterials, and may provide road maps to future innovations in nanoscale optical devices, components, and more intricate nanoscale metamaterials.

In microelectronics, the notion of a circuit is a powerful concept in which a flow of a certain quantity (e.g., electric current as the “flow” of charges) is related to a potential of another quantity (e.g., electric potential) through the functions of “lumped” elements (e.g., resistor, inductor, capacitor, diode). This “lumpedness” of circuit elements is an important assumption in modeling, allowing simplification and, effectively, modularization of the function of each element. From a systems point of view, in effect what is happening inside the element becomes less relevant to the connectivity and functionality of this modularized element to the rest of the system. This notion has been extensively and successfully used in the radio frequency (RF) and microwave domains and has been proven to be a powerful tool in the design, innovation, and discovery of new functionalities in circuits in those frequency domains. Extending the operating frequency to higher frequency regimes—for example, terahertz, infrared (IR), and visible wavelengths—may in general lead to miniaturization of devices, higher storage capacities, and larger data transfer rates. Therefore, a natural question may be asked: Can this concept of lumped circuit elements, and the mathematical machinery and tools of circuit theory, be extended and applied to the optical domain? Initially, one may imagine that merely scaling down the sizes of elements from the microwave to optical wavelengths may achieve this goal. However, several obstacles must be overcome before such optical lumped elements can be conceived. The first challenge is the size of such an optical module. Just as circuits in the lower frequency domains (e.g., in RF and microwave domains) indeed involve elements that are

much smaller than the wavelength of operation, fabrication techniques can be used to construct nanoparticles with subwavelength dimensions at optical wavelengths. Therefore, the obstacle of size reduction may be overcome. The second, more limiting, hurdle is the response of metals at IR and optical frequencies, which cannot be simply scaled from RF to optics. Metals such as gold,

silver, aluminum, and copper are highly conductive materials at RF and microwaves and consequently are commonly used in many circuits in these regimes. However, at optical frequencies, some noble metals behave differently in that they do not exhibit conductivity in the usual sense but instead exhibit plasmonic resonance (i.e., coupling of optical signals with collective oscillation of conduction electrons at these metal surfaces) as a result of the negative real part of their permittivities. Therefore, clearly, at optical wavelengths the conduction current may not be the main current flowing in such lumped optical elements. Instead, the other well-known current term, which arises from the Maxwell equations, that is, the electric displacement current density $\frac{\partial D}{\partial t}$, can be used as the “flowing optical current.” Therefore, just scaling down the element size may not provide answers to the above questions.

Lumped Optical Nanoelements

With these issues in mind, my group took an entirely different approach to address the above questions (1). Imagine a deeply subwavelength-size nanoparticle made of a nonmagnetic material with permittivity ϵ illuminated with a monochromatic optical signal with angular frequency ω (Fig. 1A) (2). After solving the Maxwell equations for the optical electric and magnetic vector fields inside and near this small particle, one can specify and evaluate the optical electric

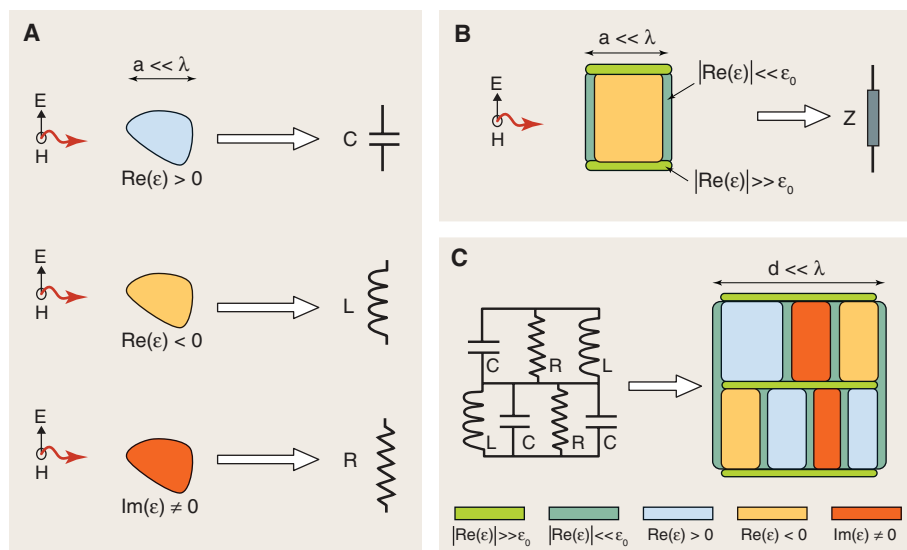


Fig. 1. Subwavelength nanoparticles as lumped nanocircuit elements at optical frequencies, and the collections of such nanoparticles. (A) A nanoparticle, with subwavelength size, when illuminated by a monochromatic optical signal, can effectively play the role of a lumped optical circuit element, depending on the permittivity of its material (2). (B) An optical nanomodule, formed by a material nanoparticle with subwavelength size, covered on its sides by layers of material with a very low real part of relative permittivity and on its two ends by layers of material with a very high real part of relative permittivity. This may perform as an insulated, lumped optical nanoelement with two connecting terminals. (C) Illustration of the concept of mn-circuits, several lumped optical nanomodules of (B), arranged next to each other, with a subwavelength dimension. When this mn-circuit is excited by an optical signal, the optical electric fields and displacement currents in these elements are tailored and patterned such that this collection of particles may behave approximately as the circuit shown on the left in a specific frequency band.

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displacement current flowing into and out of this particle, and because the particle is small compared with the wavelength one can also define an averaged optical electric potential across this particle (1, 2). The ratio of these two quantities, optical potential to displacement current, can then be assigned as the optical “lumped impedance” of this nanoparticle. Such an impedance is clearly dependent on the shape and size of the particle, the materials forming the particle, the optical frequency, and possibly its orientation with respect to the impressed optical electric field. It turns out that the choice of material can determine the type of lumped impedance the nano-

particle may represent (1): If the material is a conventional dielectric (e.g., SiO₂ or Si) with $\text{Re}(\epsilon) > 0$ at optical frequencies, the nanoparticle will act as a capacitive impedance (i.e., nanocapacitor); if, however, the particle is made of material with $\text{Re}(\epsilon) < 0$ at optical wavelengths (e.g., noble metals such as Ag and Au), the particle may behave as a negatively capacitive impedance, which implies that it will behave as an inductive impedance (i.e., nanoinductor) (3); and when the material exhibits some material loss, that is, when its $\text{Im}(\epsilon) \neq 0$ (which is almost always the case), a “nanoresistor” element should be included in the nanocircuit representation of

the nanoparticle. This behavior is consistent with the dispersion properties of dielectric functions of optical materials discussed in (4). Other nonlinear lumped elements, such as an optical lumped nanorectifier-nanodiode, may also be envisioned when nonlinear optical materials are mixed with plasmonic nanoparticles. Before moving forward toward such optical nanocircuits, we need to expand on the analogy with conventional RF circuits. In standard RF circuits, the individual lumped elements are insulated from each other by nonconducting insulating materials (e.g., dielectric or air) and are connected to other elements only at their terminals using conducting wires. In short, one does not usually have to be concerned about the leakage of conduction current from the middle of the lumped elements. In the optical domain, however, the optical electric displacement current in the nanoparticles considered here can in general leak into and out of different parts of the nanoparticle surface. This current leakage, which can lead to coupling among various tightly packed nanoelements, can be accounted for as dependent sources in the circuit paradigm (1). To strengthen the analogy between the two paradigms of the conventional RF circuits and the optical nanocircuits envisioned here, we have proposed the use of additional thin layers of materials with proper values of permittivity around the nanoparticles (5). For these layers to act as “insulators” for the optical displacement current, that is, to allow negligibly small displacement current and to stop the leakage, the real part of their relative permittivities needs to be very small. Such “epsilon-near-zero” (ENZ) materials, if designed properly, should prevent leakage of the optical electric displacement current, because inside such materials the displacement vector \mathbf{D} should be negligibly small for a finite electric field. On the other hand, if one wants layers of materials that allow an easy flow of displacement current without introducing a noticeable optical electric field, materials with high relative real part of permittivity should be considered, because in such high-permittivity media a very small electric field can produce a high amount of displacement current. Such “epsilon-very-large” (EVL) materials can play the role of nanoscale “conduit” for the optical displacement current, analogous to the role that metallic wires play for the conduction current in the RF domains. Now let us consider a sub-wavelength nanoparticle that has a thin layer of an ENZ material around its sides and thin layers of EVL materials on its two ends (Fig. 1B). Such a composite nanoparticle can allow the flow of the optical displacement current in and out of its two EVL terminals and yet confine this current within it without any leakage from its ENZ side (5). Depending on the permittivity of the main material in the particle, this composite nanostructure can indeed act approximately as a modularized lumped nanoelement at optical frequencies. Thus, the addition of the ENZ and EVL materials for shielding and connecting the nanoparticle, although not always necessary, can provide us with

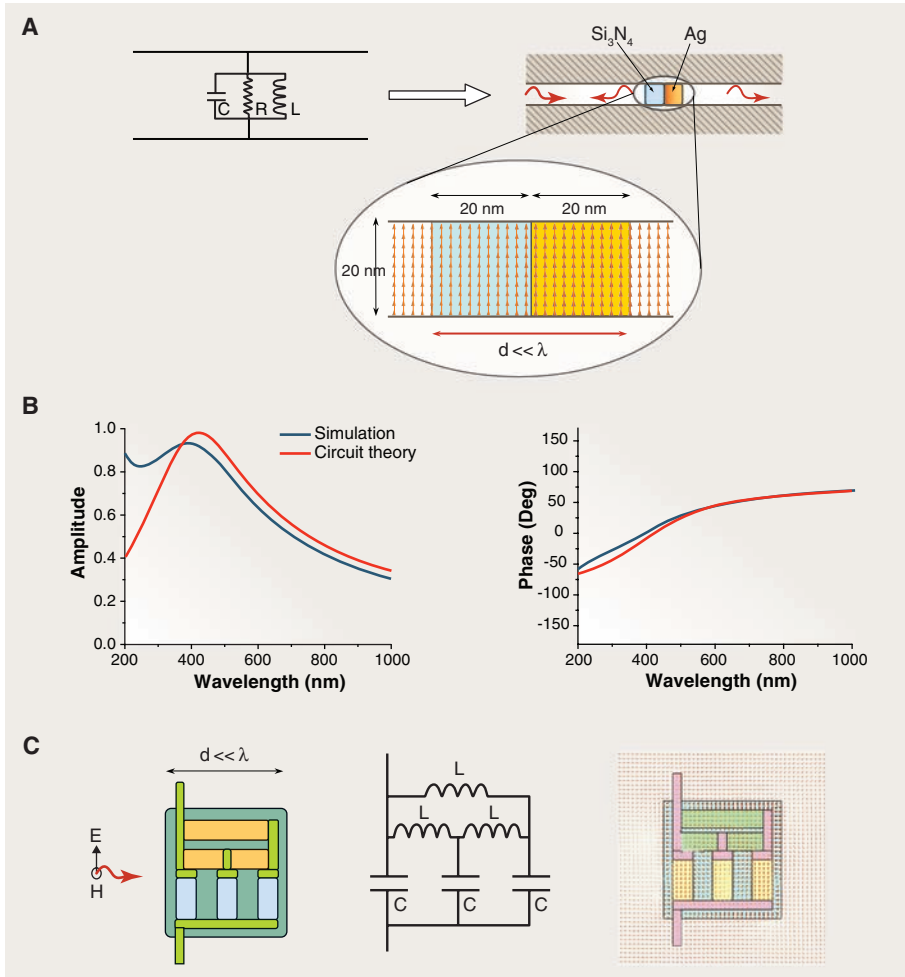


Fig. 2. Designed functionality: an example of filtering properties of optical mn-circuits. (A) RF circuit on the left shows a standard band-pass RLC filter; the mn-circuit on the right shows the cross section of a 2D optical counterpart of such nanofilters, formed by juxtaposing two nanorods, one made of Si₃N₄ with permittivity of $\sim 4.33\epsilon_0$ and the other made of Ag with a Drude model dispersion consistent with the silver permittivity data from the literature. The inset shows the zoomed-in 2D full-wave numerical simulation of optical electric field vectors, when a 421-nm-wavelength optical signal guided in this waveguide impinges on these two nanorods. (B) Amplitude and phase of the transfer function of the 2D nanofilter shown in (A). In each plot, the two curves are shown, one representing the full-wave 2D simulation of the nanorod collection (black) and the other the result of the lumped circuit theory (red). The good agreement between the two curves supports the notion that the two nanorods indeed effectively act as lumped elements. (C) A cross section of a more complex 2D mn-circuit formed by six nanoelements (three nanoinductors and three nanocapacitors) is sketched in the left (color codes as in Fig. 1C), representing the circuit shown in the middle panel. A snapshot of optical electric field distribution in this cross section, when the mn-circuit is excited by a plane wave from the left, is obtained using the full-wave 2D numerical simulation and is shown on the right.

a closer analogy between the RF and the optical circuit concepts and can also lead to lumped impedance values that would effectively be independent of the orientation of this nanomodule with respect to the impressed optical electric field (5). Before discussing how various arrangements of such nanoparticles positioned next to one another can give us functional optical nanocircuits, I need to mention the role of metamaterials in this paradigm.

Metamaterials

Metamaterials are engineered composite media, formed by packing and embedding various subwavelength inclusions and inhomogeneities, which can exhibit unconventional response functions not observed in their individual constituents or in natural media, such as negative, low, or near-zero permittivities or permeabilities. When both permittivity and permeability are negative at a given frequency, the result is a negative refractive index (6). Metamaterials, particularly those with negative refraction, have attracted a great deal of interest in recent years (7–26). After the first experimental verification of a metamaterial with negative refraction at microwave frequencies (13), inspired by the work of Pendry on split-ring resonators (14), experimental and theoretical development of this area started in the microwave regime and has been steadily moving into the higher frequency regime, with recent experimental breakthroughs in the THz, infrared, and visible ranges (15–20). It is important to emphasize that the concept of metamaterials is not limited to the negative-index phenomenon. Indeed, other artificially engineered materials with unusual parameter values, such as ENZ materials (21, 22), EVL materials (5, 23), and single-negative (SNG) media, may offer exciting potential applications as well. For instance, using ENZ materials, we have theoretically shown the possibility of squeezing light through very narrow channels and tight bends (21), as well as its role in transparency and cloaking (22, 25). Broadly speaking, metamaterials provide a platform for dispersion engineering and management, namely, the possibility of developing materials with desired temporal and spatial dispersions, which would provide powerful tools in manipulating and tailoring electromagnetic waves. For instance, it is well known that by stacking pairs of thin layers of plasmonic material (e.g., Ag) and conventional dielectric, one can form an anisotropic metamaterial whose permittivity tensor elements can achieve near zero or very high values (27–29). This suggests an example for our ENZ and EVL materials around the nanoelements.

A Tapestry of Nanostructures: “Metananocircuits”

For our optical nanocircuit elements, metamaterials, including plasmonic media, play important roles in the development of this concept. Using the notion of optical nanomodules described

above, let us now imagine that one can position next to each other a set of these lumped nanoelements, each of deeply subwavelength size and composed of specific materials (2). This tapestry of composite nanoparticles as optical nanomodules indeed forms a new paradigm as an optical

pattern of local optical electric and displacement vector fields that is analogous to the pattern of voltage and current distributions in a conventional RF circuit (Fig. 1C). This circuit can be excited by an optical signal through various means, such as optical nanoantennas or optical plasmonic waveguides feeding this circuit, or direct optical illuminations. The arrangement of nanomodules can be used to tailor the local optical electric and displacement vector fields in a desired manner in a subwavelength domain, analogous to the way, on an RF test bench in an electronic circuit laboratory, one connects different conventional circuit elements by using conducting wires on a circuit board. I argue that this patterning of local optical field can, under proper conditions, provide us with functionalities for information processing (e.g., low-pass, high-pass, or band-pass filtering), as a regular circuit does in the RF domain. Let us take the case of a filter with a two-dimensional (2D) geometry as an example (Fig. 2A). In the RF domain, a simple conventional band-pass (or band-stop) filter can be designed using a parallel (or series) combination of an inductor (L), a capacitor (C), and a resistor (R). If we want to have an analogous filter function in our optical mn-circuit, we will need to use two nanomodules—one nanoparticle (or nanorod in this 2D case) made of a material with negative permittivity (e.g., plasmonic materials such as noble metals) acting as a nano-inductor accompanied by a nano-resistor due to the material loss, and the other nanoparticle formed by a dielectric material acting as a nanocapacitor. With proper design, juxtaposing these two nanomodules, either in parallel or in series, may provide us with an optical mn-circuit with, respectively, the band-pass or the band-stop filtering functionality at a certain range of optical wavelengths. For the parallel case with 2D geometry (Fig. 2A), this assertion has been shown numerically using full-wave simulations of Maxwell equations, when a Drude dispersion model is assumed for the plasmonic material (e.g., Ag) forming the nano-inductor module (including material loss representing a nanoresistor) and a simple dielectric permittivity and a simple dielectric permittivity is assumed for the nanocapacitor module. This 2D nanofilter is placed within a thin parallel-plate waveguide with impenetrable walls at the top

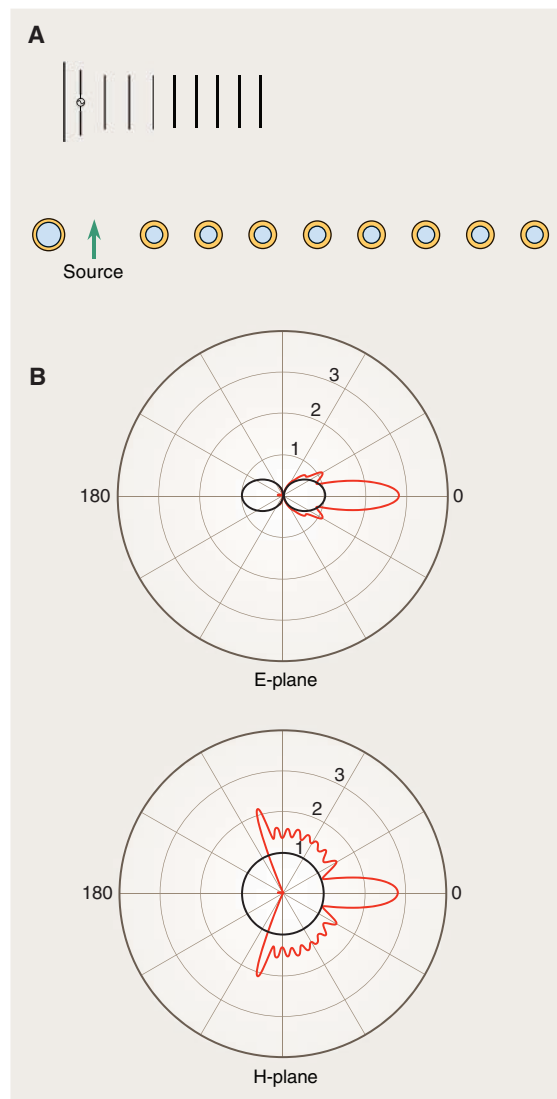


Fig. 3. Metananocircuit as a tool in the design of optical Yagi-Uda nanoantennas (30). (A) A sketch of conventional Yagi-Uda RF antenna is shown above. The collection of shell particles (with two different ratios of radii) around an optical point dipole source (e.g., a molecule) can form Yagi-Uda-type optical nanoarrays. (B) The theoretically evaluated radiation patterns of the optical Yagi-Uda-like nanoarrays in (A) at 620 nm (red), compared with that of a dipole alone (black). In (30), we used the core of SiO₂ and the shell of Ag in our analysis, with outer radius of $0.2\lambda_0$ and ratios of radii of 0.851 and 0.834 for the left and right nanoshells, respectively. The distance between the left nanoshell and the source is $0.25\lambda_0$, while that on the right (and between the right particles) is $0.65\lambda_0$. [From (30)].

nanocircuit with subwavelength dimensions (Fig. 1C). Such a “metananocircuit” (mn-circuit), when excited by an optical signal, manifests a

is assumed for the nanocapacitor module. This 2D nanofilter is placed within a thin parallel-plate waveguide with impenetrable walls at the top

and bottom [thus supporting a transverse electromagnetic (TEM) mode], acting as a two-port network. The transfer function of this filter, that is, the ratio of the optical potential at the output port to that of the incoming potential, shows a band-pass behavior, which confirms our approach to this nanofilter design at optical wavelengths (Fig. 2B). (The dispersion of the waveguide alone is excluded.) More complex nanocircuits can be envisioned when more than two nanomaterials can be arranged, providing higher order transfer function for such circuits. The left panel of Fig. 2C presents the cross section of another 2D example with six optical nanoelements in a specific layout, providing the functionality essentially analogous to that of the circuit shown in the middle panel of Fig. 2C. In the right panel, we see that the full-wave 2D simulation of a snapshot of the optical electric vector field in the cross section of this 2D mn-circuit reveals field patterns that are analogous to voltage distributions in the circuit. Various material dispersions used in such mn-circuits can provide an even richer variety of transfer functions beyond the conventional RF counterparts. The performance and quality factors of such optical nanocircuit elements depend on the relative values of real and imaginary parts of permittivities of materials in the range of operating wavelengths and, therefore, depending on specific scenarios and applications, it may be preferable to use optical materials with proper ranges of ratios of imaginary to real parts of permittivity.

Although the concept of mn-circuits is based on the arrangement of metamaterial and plas-

monic nanostructures, the converse may also be considered, namely, these optical mn-circuits can be envisioned as lumped inclusions to be used for synthesizing metamaterials with prescribed, and even more intricate, dispersion properties. As in the case of microwave metamaterials in which distributions of resonant elements [for instance, either split-ring (L-C) resonators in the 3D realizations (13) or lumped RF circuit elements (e.g., lumped inductors and capacitors) in the planar transmission line metamaterials (10, 11)] are considered, here optical mn-circuits can be the building blocks as inclusions for more diverse classes of engineered materials in the future, providing a road map for tailoring novel optical metamaterials with various dispersion features.

Designing Optical Nanodevices and Components

To illustrate how such mn-circuits may contribute to the understanding and innovation of other nano-optical devices and components, we have studied and analyzed several problems in which these concepts can provide guides to solutions. One such problem is how some of the well-known antenna designs in the RF and microwave domains, for example, the Yagi-Uda antennas, can be brought into the nanoscale optical domain (30). In the Yagi-Uda antenna, the main element is known to be a resonant dipole, accompanied by several parasitic (i.e., passive) wire elements in order to narrow the antenna radiation patterns and point the main beam in a given direction (Fig. 3). To transplant this concept from the microwave into the optical domain, in (30) we considered two-material nanostructures [e.g.,

nanoshell particle with dielectric core and plasmonic shell (31)] resembling resistor-inductor-capacitor (RLC) resonant circuit at optical frequencies. It is known that at a particular ratio of core-to-shell radii, this particle is at resonance (31, 32). Figure 3A shows this idea where several nanoshell particles, with a core of SiO₂ and a shell of Ag and a certain ratio of radii, are placed at the right side of an optical point-dipole source (e.g., a quantum dot or a fluorescent molecule), and a single similar nanoshell particle but with a different ratio of radii is situated at the left side of this source (30). The radiation pattern of this nanoantenna, as obtained from our theoretical analysis (30), may indeed, under proper conditions, show a right-pointed main beam that is narrower than that of a single dipole, as expected and anticipated from such an antenna array (Fig. 3B). Therefore, the presence of these nanoparticles in the vicinity of the optical source, for example, a molecule, can indeed affect its emission properties. Because this design is sensitive to the operating wavelength, one can envision a set of several optical Yagi-Uda nanoantennas coupled to the same molecule, but each designed for a different specific wavelength and placed at a different orientation around a molecule. In such a scenario, each nanoantenna array, which is optimized for a specific wavelength, has its main beam pointed in a different direction. This set-up will analyze the spectral information of the molecular emission and transform the spectral contents into specific angular variations of emitted signals.

Another topic that has received inspiration from this concept of mn-circuits is the theory we

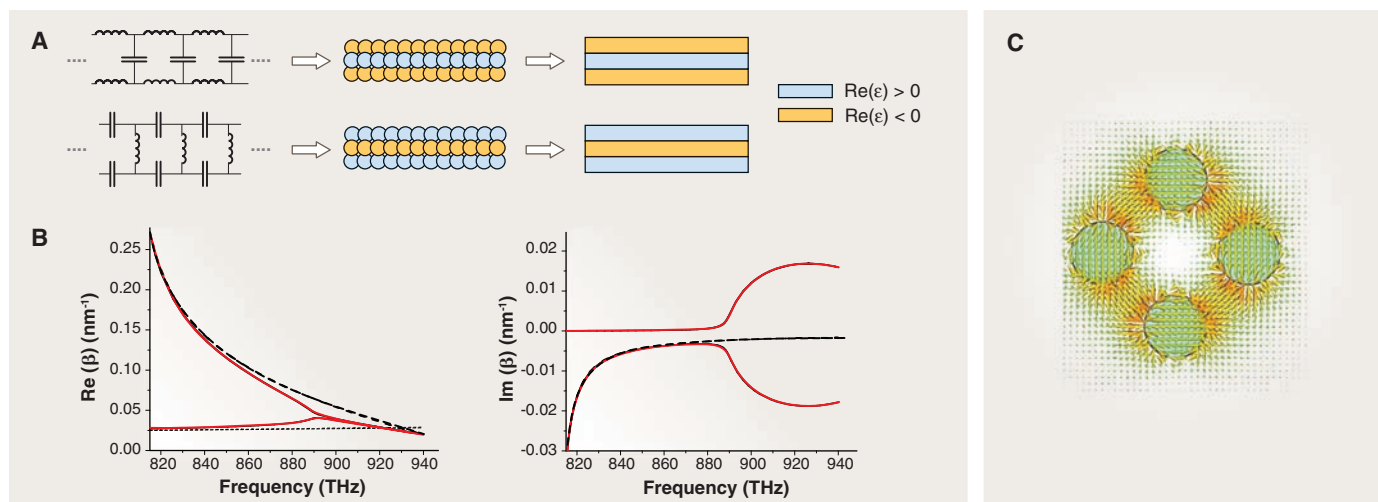


Fig. 4. Optical nanotransmission line based on the mn-circuits. (A) The concept of transmission lines in RF and microwave (left) can be brought into the optical domain using the notion of lumped nanocircuit elements (middle and right). By replacing the lumped inductor and capacitor with plasmonic [Re(ε) < 0] and dielectric [Re(ε) > 0] nanoparticles, respectively, the structures shown in the middle panel can be obtained. In the limit, when these nanoparticles merge into each other, the guided-wave structures sketched on the right are the result. These structures thus indeed function as optical nanotransmission (37). (B) The dispersion diagram of the waveguide shown in (A), when the SiO₂ and

Ag are considered for the dielectric and plasmonic materials. Solid lines are for the even mode in Ag-SiO₂-Ag waveguide; dashed lines are for the odd mode in SiO₂-Ag-SiO₂ waveguide; the dotted line shows the light line for SiO₂. For Ag, a Drude dispersion is assumed in our analysis. These results show that such optical nanotransmission lines can exhibit backward-wave and forward-wave propagation, as their RF and microwave counterparts do. [Adapted from (37). Copyright 2006, Optical Society of America] (C) Simulated electric field distribution for a nanoring composed of four plasmonic nanospheres at 655 THz. [Adapted from (41). Copyright 2006, Optical Society of America]

developed for the far-field subdiffraction optical microscopy (FSOM), or supermicroscopy (29). In this technique, an optical imaging system in the far field can in principle capture the image of two points that are placed less than half a wavelength from each other. An ordinary microscope cannot resolve two such points because of the Abbe-Rayleigh limit. However, in the theory of FSOM, we have shown that by using properly designed metamaterial crystals in the close vicinity of the object, one can magnify these objects in the near field such that their images in the output plane of the metamaterial crystal structure can be farther apart than half a wavelength, and then a regular optical microscope can detect these magnified images. Thus, the overall imaging system can in principle have a resolution better than the conventional Abbe-Rayleigh limit, although it is still a far-field system with a near-field magnification. The key section of such FSOM is the metamaterial layered structure in which stacks of pairs of thin plasmonic and dielectric layers create a medium with hyperbolic dispersion. The permittivity tensor of such a structure is similar to that of anisotropic plasma, which has been investigated by many groups. An interesting feature in wave propagation in such a medium is the cone of resonance (33). Balmain's group (33) has studied this phenomenon by analyzing two-dimensional arrays of lumped inductors and capacitors in the microwave frequencies. We investigated what would happen if we replaced their RF lumped inductors and capacitors with our optical lumped nanoinductors and nanocapacitors using negative permittivity and dielectric nanoparticles, respectively. In the limit when these nanoparticles are packed closer and closer, one would obtain the metamaterial-layered structure with hyperbolic dispersion required for supermicroscopy. It is important to note that Narimanov's group, independently and at the same time but using a quite different approach, studied such metamaterial structures for supermicroscopy, which they name "hyperlens" (34). Zhang's group (35) and Smolyaninov's group (36) have experimentally verified and validated this concept.

One more topic that got inspiration from the notion of mn-circuits is the possibility of the design of 1D, 2D, and 3D optical nanotransmission lines with negative refraction (26, 37, 38). In the RF and microwave domains, it has been shown by several groups (10, 11) that dual transmission lines, formed by series lumped inductors and shunt lumped capacitors, support wave propagation with negative refraction. When one replaces these lumped elements with their optical counterparts (Fig. 1A), optical nanotransmission lines can be envisioned in which a subset of the allowed modes of propagation may exhibit negative refraction. Figure 4 sketches this concept. This approach provides an interesting way to

obtain negative refraction at optical frequencies. Atwater's group has recently demonstrated experimentally the negative refraction in 2D metal-insulator-metal geometry (39). The circuit concept has also facilitated the understanding and calculation of resonant metamaterials at optical frequencies in (40). Moreover, the concept of mn-circuits has helped to suggest the arrangements of rings of metallic nanoparticles, as circular loops of LC elements in optics, that is, the optical version of slit-ring resonators, which can generate magnetic dipole moments at optical frequencies (Fig. 4C) (41). Such rings of nanoparticles can be the basic inclusions for photonic metamaterials with magnetic response and negative refraction (41).

Concluding Remarks

Although mn-circuits may offer exciting possibilities and may suggest new ways of tackling nano-optical data processing, they also bring new challenges and questions. As the few examples described above suggest, this notion may lead to a different method in exploring some of the future potentials in nano-optics. This concept may link together the fields of circuit designs and nano-optics, along with metamaterials and plasmonics, linking the macroworld to the nanoworld in optics and electronics, and leading to metatronics as another paradigm for nanoelectronics/nanophotonics. It can open doors to the exporting and transplanting of various ideas from RF and microwave into the IR and visible frequency domains, and it may lead to innovation in nanodevices and components—with the capability of optical detection, optical processing and storage, and data exchange on the nanoscale—and to potential applications and breakthroughs in various scientific fields.

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- Although the nanoparticles are assumed to be deeply subwavelength, they are not too small to necessitate taking into account the quantum effects in these phenomena. Therefore, we are still operating in the domain of classical electrodynamics, and permittivity functions are considered.
- Depending on the frequency dispersion of the dielectric function, such an effective nanoinductor may itself be frequency dependent as $L_{\text{eff}} \propto \frac{1}{-\omega^2 a \text{Re}(\epsilon(\omega))}$, where a is length scale related to the size of particle. If we consider a Drude model for $\epsilon = \epsilon_0 \left(1 - \frac{\omega_p^2}{\omega^2}\right)$ and if we operate at frequency ω sufficiently lower than ω_p , then L_{eff} will be approximately constant. If we are close to, but still lower than, ω_p , this nanoparticle can be regarded as a parallel combination of a capacitor and an inductor, with inductive impedance still dominating the effect. I thank S. Tretyakov of Helsinki University of Technology for his comments on this latter issue and the related fruitful discussion.
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