

$$\textcircled{1} \quad (a) \quad m_H v_{H,\text{initial}} + m_{He} v_{He,\text{initial}} = m_H v_{H,\text{final}} + m_{He} v_{He,\text{final}}$$

With $v_{He,\text{initial}} = 0$,

$$v_{He,\text{final}} = \frac{m_H(v_{H,\text{initial}} - v_{H,\text{final}})}{m_{He}} = \frac{(1.674 \times 10^{-27} \text{ kg})[(1.1250 \times 10^7 \text{ m/s}) - (-6.724 \times 10^6 \text{ m/s})]}{6.646 \times 10^{-27} \text{ kg}}$$

$$= 4.527 \times 10^6 \text{ m/s}$$

$$(b) \quad \frac{1}{2} m_H v_{H,\text{initial}}^2 + \frac{1}{2} m_{He} v_{He,\text{initial}}^2 = \frac{1}{2} m_H v_{H,\text{final}}^2 + \frac{1}{2} m_{He} v_{He,\text{final}}^2$$

$$v_{He,\text{final}} = \sqrt{\frac{m_H(v_{H,\text{initial}}^2 - v_{H,\text{final}}^2)}{m_{He}}}$$

$$= \sqrt{\frac{(1.674 \times 10^{-27} \text{ kg})[(1.1250 \times 10^7 \text{ m/s})^2 - (-6.724 \times 10^6 \text{ m/s})^2]}{6.646 \times 10^{-27} \text{ kg}}}$$

$$= 4.527 \times 10^6 \text{ m/s}$$

$$\textcircled{2} \quad p_i = p_f \Rightarrow (8.0 \text{ kg})(2.0 \text{ m/s}) = (4.0 \text{ kg})v_1 + (4.0 \text{ kg})v_2 \Rightarrow 4 = v_1 + v_2$$

$$K_i + \Delta K = K_f \Rightarrow \frac{1}{2}(8.0 \text{ kg})(2.0 \text{ m/s})^2 + 16 \text{ J} = \frac{1}{2}(4.0 \text{ kg})(v_1^2) + \frac{1}{2}(4.0 \text{ kg})(v_2^2)$$

$$\Rightarrow 16 = v_1^2 + v_2^2$$

$$16 = v_1^2 + (4 - v_1)^2 = v_1^2 + 16 - 8v_1 + v_1^2$$

$$0 = 2v_1^2 - 8v_1 \Rightarrow v_1 = 0, 4.0 \text{ m/s}$$

$$p_i = (8.0 \text{ kg})(2.0 \text{ m/s}) = 16 \text{ kg} \cdot \text{m/s}$$

$$p_f = (4.0 \text{ kg})(0) + (4.0 \text{ kg})(4.0 \text{ m/s}) = 16 \text{ kg} \cdot \text{m/s}$$

$$K_i = \frac{1}{2}(8.0 \text{ kg})(2.0 \text{ m/s})^2 = 16 \text{ J}$$

$$K_f = \frac{1}{2}(4.0 \text{ kg})(0) + \frac{1}{2}(4.0 \text{ kg})(4.0 \text{ m/s})^2 = 32 \text{ J} = K_i + 16 \text{ J}$$

$$③ p_i = p_f \Rightarrow m_1 v_1 + m_2 v_2 = (m_1 + m_2) v_f$$

$$\text{With } v_2 = 0, \quad m_1 v_1 = (m_1 + m_2) v_f \quad \text{or} \quad v_f = \frac{m_1}{m_1 + m_2} v_1$$

$$K_i = \frac{1}{2} m_1 v_1^2 \quad K_f = \frac{1}{2} (m_1 + m_2) v_f^2 = 0.73 K_i = 0.73 \left(\frac{1}{2} m_1 v_1^2 \right)$$

$$\frac{1}{2} (m_1 + m_2) \left[\frac{m_1}{m_1 + m_2} v_1 \right]^2 = 0.73 \left(\frac{1}{2} m_1 v_1^2 \right)$$

$$\frac{m_1^2}{m_1 + m_2} = 0.73 m_1 \quad m_1 = 0.73 (m_1 + m_2)$$

$$m_2 = \frac{m_1}{0.73} - m_1 = 0.370 m_1 = \underline{\underline{12.9 \text{ tons}}}$$