

Solutions to Practice Problems

$$\textcircled{1} \quad E_{\text{init}} = K_{\text{init}} + U_{\text{init}} = 0 + \frac{1}{2} k x_{\text{init}}^2 = 0.225 \text{ J}$$

$$E_{\text{final}} = K_{\text{final}} + U_{\text{final}} = 0 + \frac{1}{2} k x_{\text{final}}^2 = 0.048 \text{ J}$$

$$W = E_{\text{final}} - E_{\text{init}} = -0.177 \text{ J}$$

$$\textcircled{2} \quad E_i = K_i + U_i = \frac{1}{2} m v^2 + mgh = \frac{1}{2} (1520 \text{ kg}) (25 \text{ m/s})^2 + (500 \text{ kg}) (9.8 \frac{\text{m}}{\text{s}^2}) (200 \sin 20^\circ) = 1.47 \times 10^6 \text{ J}$$

$$E_f = K_f + U_f = \frac{1}{2} m v^2 = \frac{1}{2} (1520 \text{ kg}) (17 \text{ m/s})^2 = 0.216 \times 10^6 \text{ J}$$

$$W = E_f - E_i = -1.26 \times 10^6 \text{ J}$$

$$\textcircled{3} \quad \text{Initial: } K=0, \quad U_{\text{grav}}=0, \quad U_{\text{spring}}=0$$

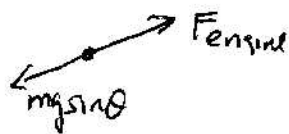
$$\text{Final: } K=0, \quad U_{\text{grav}}=-mgh, \quad U_{\text{spring}} = \frac{1}{2} k (h-L)^2$$

$$E_{\text{init}} = E_{\text{final}} \Rightarrow 0 = -mgh + \frac{1}{2} k (h-L)^2$$

$$\frac{1}{2} k h^2 - kLh - mgh + \frac{1}{2} k L^2 = 0$$

$$\text{Solve using quadratic formula} \Rightarrow h = 28.8 \text{ m}$$

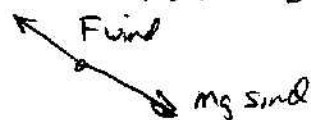
$\textcircled{4} \quad (a)$



$$P = F_{\text{engine}} \cdot v = (mg \sin \theta) (v) = 20 \text{ kW}$$

$$\text{total power} = 20 \text{ kW} + 16 \text{ kW} = 36 \text{ kW}$$

(b) The effective force of wind resistance is $F = \frac{P}{v} = \frac{16,000 \text{ W}}{15 \text{ m/s}} = 1067 \text{ N}$



$$F_{\text{wind}} = mg \sin \theta \quad \text{at constant speed.}$$

$$\sin \theta = \frac{F_{\text{wind}}}{mg} = 0.064 \Rightarrow \theta = 3.7^\circ$$