

## MATLAB NOTES

Matlab designed for numerical computing.

Strongly oriented towards use of arrays, one and two dimensional.

Excellent graphics that are easy to use.

Powerful interactive facilities; and programs can also be written in it.

It is a procedural language, not an object-oriented language.

It has facilities for working with both Fortran and C language programs.

## USING MATLAB

At the prompt in Unix, type *Matlab*. Or use the pull down menu accessed with the right button.

Run the *Demo* program (simply type *demo*).

To seek help on any command, simply type

*help command*

To seek information on Matlab commands that involve a given *word* in their description, type

*lookfor word*

Look at the various online manuals available thru the course web page.

*MATLAB* is an interactive computer language. For example, to evaluate

$$y = 6 - 4x + 7x^2 - 3x^5 + \frac{3}{x+2}$$

use

$$y = 6 - 4*x + 7*x*x - 3*x^5 + 3/(x+2);$$

There are many built-in functions, e.g.

$$\exp(x), \cos(x), \text{sqrt}(x), \log(x)$$

The default arithmetic used in *MATLAB* is double precision and real. However, complex arithmetic appears automatically when needed.  $\text{sqrt}(-4)$  results in an answer of  $2i$ .

The default output to the screen is to have 4 digits to the right of the decimal point. To control the formatting of output to the screen, use the command `format`. The default formatting is obtained using

```
format short
```

To obtain the full accuracy available in a number, you can use

```
format long
```

The commands

```
format short e
```

```
format long e
```

will use 'scientific notation' for the output. Other `format` options are also available.

*MATLAB* works very efficiently with arrays, and many tasks are best done with arrays. For example, plot  $\sin x$  and  $\cos x$  on the interval  $0 \leq x \leq 10$ .

```
t = 0:.1:10;  
x = cos(t); y = sin(t);  
plot(t,x,t,y)
```

The statement

```
t = a:h:b;
```

with  $h > 0$  creates a row vector of the form

$$t = [a, a + h, a + 2h, \dots]$$

giving all values  $a + jh$  that are  $\leq b$ .

When  $h$  is omitted, it is assumed to be 1. Thus

```
n = 1:5
```

creates the row vector

$$n = [1, 2, 3, 4, 5]$$

## ARRAYS

$$b = [1, 2, 3]$$

creates a row vector of length 3.

$$A = [1\ 2\ 3; 4\ 5\ 6; 7\ 8\ 9]$$

creates the square matrix

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

Spaces or commas can be used as delimiters in giving the components of an array; and a semicolon will separate the various rows of a matrix. For a column vector,

$$b = [1\ 3\ -6]'$$

results in the column vector

$$\begin{bmatrix} 1 \\ 3 \\ -6 \end{bmatrix}$$

## ARRAY OPERATIONS

**Addition:** Do componentwise addition.

$$A = [1, 2; 3, -2; -6, 1];$$

$$B = [2, 3; -3, 2; 2, -2];$$

$$C = A + B;$$

results in the answer

$$C = \begin{bmatrix} 3 & 5 \\ 0 & 0 \\ -4 & -1 \end{bmatrix}$$

**Multiplication by a constant:** Multiply the constant times each component of the array.

$$D = 2*A;$$

results in the answer

$$D = \begin{bmatrix} 2 & 4 \\ 6 & -4 \\ -12 & 2 \end{bmatrix}$$

**Matrix multiplication:** This has the standard meaning.

$$E = [1, -2; 2, -1; -3, 2];$$

$$F = [2, -1, 3; -1, 2, 3];$$

$$G = E * F;$$

results in the answer

$$G = \begin{bmatrix} 1 & -2 \\ 2 & -1 \\ -3 & 2 \end{bmatrix} \begin{bmatrix} 2 & -1 & 3 \\ -1 & 2 & 3 \end{bmatrix} = \begin{bmatrix} 4 & -5 & -3 \\ 5 & -4 & 3 \\ -8 & 7 & -3 \end{bmatrix}$$

**A nonstandard notation:**

$$H = 3 + F;$$

results in the computation

$$H = 3 \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} + \begin{bmatrix} 2 & -1 & 3 \\ -1 & 2 & 3 \end{bmatrix} = \begin{bmatrix} 5 & 2 & 6 \\ 2 & 5 & 6 \end{bmatrix}$$

## COMPONENTWISE OPERATIONS

Matlab has component-wise operations for multiplication, division and exponentiation. These three operations are denoted by using a period to precede the usual symbol for the operation. With

$$a = [1 \ 2 \ 3]; \quad b = [2 \ -1 \ 4];$$

we have

$$\begin{aligned} a.*b &= [2 \ -2 \ 12] \\ a./b &= [0.5 \ -2.0 \ 0.75] \\ a.^3 &= [1 \ 8 \ 27] \\ 2.^a &= [2 \ 4 \ 8] \\ b.^a &= [2 \ 1 \ 64] \end{aligned}$$

The expression

$$y = 6 - 4x + 7x^2 - 3x^5 + \frac{3}{x+2}$$

can be evaluated at all of the elements of an array  $x$  using the command

$$y = 6 - 4*x + 7*x.*x - 3*x.^5 + 3./(x+2);$$

The output  $y$  is then an array of the same size as  $x$ .

## OTHER COMMANDS

`clear`: To remove the current variables from use.

`cls`: To clear the output screen.

`help command_name`: Brief description of *command\_name*.

```
help sqrt
```

results in the output

SQRT Square root.

`SQRT(X)` is the square root of the elements of `X`. Complex results are produced if `X` is not positive.

## Special arrays:

`A = zeros(2,3)`

produces an array with 2 rows and 3 columns, with all components set to zero,

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

`B = ones(2,3)`

produces an array with 2 rows and 3 columns, with all components set to 1,

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

`eye(3)` results in the  $3 \times 3$  identity matrix,

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

## ARRAY FUNCTIONS

There are many *MATLAB* commands that operate on arrays, we include only a very few here. For a vector  $x$ , row or column, of length  $n$ , we have the following functions.

`max(x)` = maximum component of  $x$

`min(x)` = minimum component of  $x$

`abs(x)` = vector of absolute values of components of  $x$

`sum(x)` = sum of the components of  $x$

`norm(x)` =  $\sqrt{|x_1|^2 + \cdots + |x_n|^2}$

## SCRIPT FILES

A list of interactive commands can be stored as a script file.

For example, store

```
t = 0:.1:10;  
x = cos(t); y = sin(t);  
plot(t,x,t,y)
```

with the file name *plot\_trig.m*. Then to run the program, give the command

```
plot_trig
```

The variables used in the script file will be stored locally, and parameters given locally are available for use by the script file.

## FUNCTIONS

To create a function, we proceed similarly, but now there are input and output parameters. Consider a function for evaluating the polynomial

$$p(x) = a_1 + a_2x + a_3x^2 + \cdots + a_nx^{n-1}$$

*MATLAB* does not allow zero subscripts for arrays. The following function would be stored under the name `polyeval.m`. The coefficients  $\{a_j\}$  are given to the function in the array named `coef`, and the polynomial is to be evaluated at all of the components of the array `x`.

```
function value = polyeval(x,coeff);
%
% function value = polyeval(x,coeff)
%
% Evaluate a polynomial at the points given
% in x. The coefficients are to be given in
% coeff. The constant term in the polynomial
% is coeff(1).

n = length(coeff)
value = coeff(n)*ones(size(x));
for i = n-1:-1:1
value = coeff(i) + x.*value;
end
```