Power Series for Two Point Charges

Each of the power series below comes from expanding the electrostatic potential due to a pair of positive charges OR a pair of opposite charges lying along the z-axis at $\pm D$. The expansions are along either the z-axis OR the the x-axis for either large or small values of the variable z or x.

Match each series to the region where it is valid. Be prepared to explain your reasoning. Then give a physical explanation for as many terms of the series as you can.

$$1. \quad \frac{Q}{4\pi\epsilon_0} \frac{2}{D} \left(1 + \frac{z^2}{D^2} + \frac{z^4}{D^4} + \dots \right)$$

$$2. \quad 0$$

$$3. \quad \frac{Q}{4\pi\epsilon_0} \frac{2}{|x|} \left(1 - \frac{1}{2} \frac{D^2}{x^2} + \frac{3}{8} \frac{D^4}{x^4} + \dots \right)$$

$$4. \quad 0$$

$$5. \quad \frac{Q}{4\pi\epsilon_0} \frac{2}{D} \left(\frac{z}{D} + \frac{z^3}{D^3} + \frac{z^5}{D^5} + \dots \right)$$

$$6. \quad \frac{Q}{4\pi\epsilon_0} \frac{2}{|z|} \left(1 + \frac{D^2}{z^2} + \frac{D^4}{z^4} + \dots \right)$$

$$7. \quad \frac{Q}{4\pi\epsilon_0} \frac{2}{D} \left(1 - \frac{1}{2} \frac{x^2}{D^2} + \frac{3}{8} \frac{x^4}{D^4} + \dots \right)$$

$$8. \quad \frac{Q}{4\pi\epsilon_0} \frac{2}{|z|} \left(\frac{D}{z} + \frac{D^3}{z^3} + \frac{D^5}{z^5} + \dots \right)$$

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