

# La Geometría de la Teoría Especial de la Relatividad

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# The Geometry of Special Relativity

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Slides available at:

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Textbook available at:

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The laws of physics apply in all inertial reference frames.

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Can measure  $\epsilon_0$  and  $\mu_0$ , so can measure

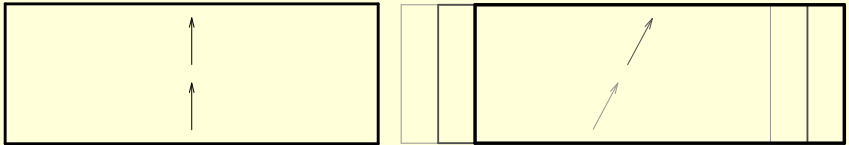
$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} = 3 \times 10^8 \frac{\text{m}}{\text{s}}$$

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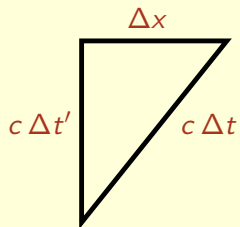
### Postulate 2:

The speed of light is the same for all inertial observers.



A beam of light bounces up and down between mirrors on the floor and ceiling of a moving train. The time between bounces can be used as a unit of time, but a moving observer and a stationary observer obtain different results.

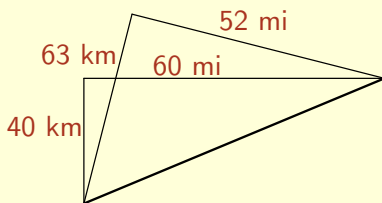




$$(c \Delta t')^2 = (c \Delta t)^2 - (\Delta x)^2$$

*Suppose a town has daytime surveyors, who determine North and East with a compass, and nighttime surveyors, who use the North Star. These notions of course differ, since magnetic north is not the direction to the North Pole. Suppose further that both groups measure north/south distances in kilometers and east/west distances in miles, with both being measured from the town center. How does one go about comparing the measurements of the two groups?*

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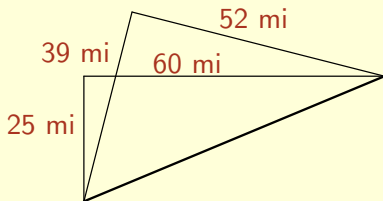


Moral:

Use the same units!

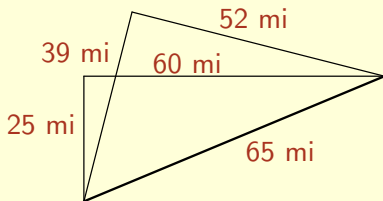
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*Draw a spacetime diagram showing yourself standing still.*



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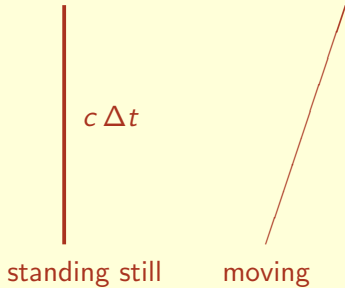
standing still

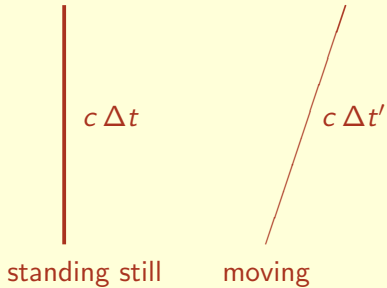


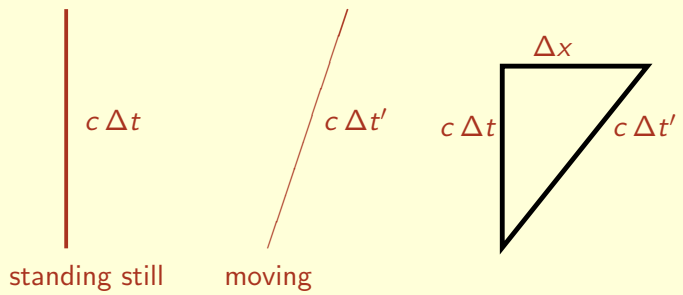
standing still

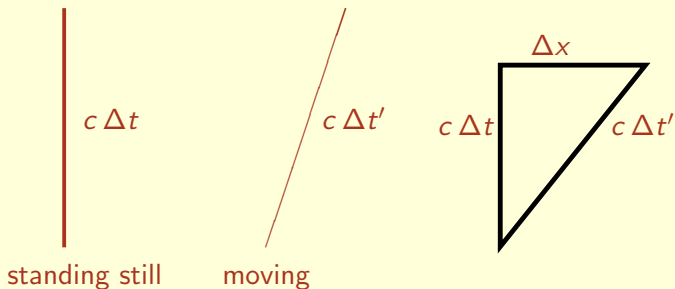


moving









$$\frac{v}{c} = \frac{\Delta x}{c \Delta t}$$

$$(c \Delta t')^2 = (c \Delta t)^2 - (\Delta x)^2$$



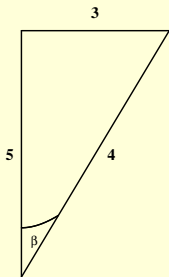
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*Draw a 3-4-5 triangle in this new geometry.*

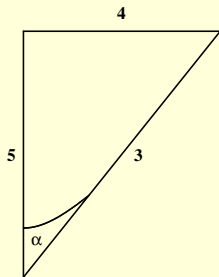
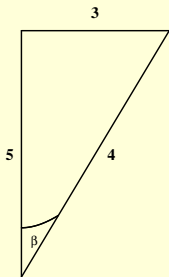
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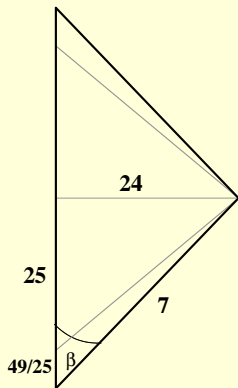
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- Moving observers measure time differently.
- Space and time should be measured in the same units.
- Times (and distances) can be measured in spacetime diagrams.
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