## CHEMISTRY 448/548 Winter 2009

Assignment \#3 (55 pts)
Due Feb. 6th

## SHOW WORKING FOR FULL CREDIT AND ALL WORK MUST BE NEAT AND READABLE OR YOU WILL LOSE POINTS !

Be careful of SF's particularly in spreadsheet o/p

1. ( 15 pts) Below is sketched an approximate potential energy curve for the dissociative adsorption of a diatomic molecule on a metal.

(a) Does this diagram show (i) physisorption, (ii) activated chemisorption or (iii) non-activated chemisorption? ( 1 pt )

Ans: (ii) activated chemisorption
(b) What are the bond lengths in the precursor and chemisorbed states? (2 pts)

Ans: precursor $=340 \mathrm{pm}$, chemisorbed $=190 \mathrm{pm}$
(c) What is the enthalpy of adsorption into the precursor and chemisorption states. (4 pts)

Ans: precursor $=-11 \mathrm{~kJ} / \mathrm{mol}$, chemisorbed $=-110 \mathrm{~kJ} / \mathrm{mol}$
(d) What is the energy of activation for chemisorption? (2 pts).

Ans: $\Delta H=39 \mathrm{~kJ} / \mathrm{mol}$
(e) What is the enthalpy of desorption as a molecule from the chemisorption state? (2 pts)

Ans: $\Delta H=110+39=150 \mathrm{~kJ} / \mathrm{mol}$
(f) What is the enthalpy of desorption from the precursor state? (1 pts)

Ans: $\Delta H=11 \mathrm{~kJ} / \mathrm{mol}$
(g) The diatomic gas used has a bond energy of $425 \mathrm{~kJ} / \mathrm{mol}$. If the atoms were to desorb without reforming the molecule, what will be the enthalpy of desorption per mole of atoms produced in the gas phase? ( 3 pts )

Ans:


Per mole of O atoms the $\Delta H_{\text {des }}=535 / 2=238 \mathrm{~kJ} / \mathrm{mol} \mathrm{A}$
2. (20 pts) Some data for the adsorption of carbon monoxide on charcoal at 273 K are given below.

| $\mathrm{p}($ torr $)$ | 100 | 200 | 300 | 400 | 500 | 600 | 700 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~V}(\mathrm{ml})$ | 10.2 | 18.6 | 25.5 | 31.5 | 36.9 | 41.6 | 46.1 |

(Assume V has been corrected to 1 atm pressure)
a) Use the associative and dissociative versions of the Langmuir isotherm to find the types of adsorption occurring. Plot on graph paper or spreadsheet/printer. Calculate $\mathrm{V}_{\mathrm{m}}$ and b ( 10 pts )

Solution :
The associative Langmuir isotherm can be written as :
$\theta=\frac{V}{V_{m}}=\frac{b P}{1+b P}$ or
$\frac{P}{V}=\frac{1}{b V_{m}}+\frac{1}{V_{m} P}$


| Assoc <br> $\mathbf{p}$ (Torr) | V(mL) | P/V |
| ---: | ---: | ---: |
| 100 | 10.2 | 9.80 |
| 200 | 18.6 | 10.8 |
| 300 | 25.5 | 11.8 |
| 400 | 31.5 | 12.7 |
| 500 | 36.9 | 13.6 |
| 600 | 41.6 | 14.4 |
| 700 | 46.1 | 15.2 |

The dissociative Langmuir isotherm is :
$\frac{\sqrt{P}}{V}=\frac{1}{b V_{m}}+\frac{1}{V_{m} \sqrt{P}}$


| Dissoc <br> $\mathbf{p ( T o r r )}$ | $\mathbf{P}^{\wedge} \mathbf{0 . 5}$ | V(mL) | $\mathbf{P}^{\wedge} \mathbf{0 . 5 / \mathbf { V }}$ |
| :--- | ---: | ---: | ---: |
| 100 | 10.0 | 10.2 | 0.980 |
| 200 | 14.1 | 18.6 | 0.760 |
| 300 | 17.3 | 25.5 | 0.679 |
| 400 | 20.0 | 31.5 | 0.635 |
| 500 | 22.4 | 36.9 | 0.606 |
| 600 | 24.5 | 41.6 | 0.589 |
| 700 | 26.5 | 46.1 | 0.574 |

Clearly the associative isotherm is the correct fit. For the associative data:
Slope $=1 / \mathrm{V}_{\mathrm{m}}=1 / 0.009024$
so $\mathrm{V}_{\mathrm{m}}=110.8 \mathrm{~mL}$
intercept $=\left(1 / b V_{m}\right)=8.987$
so $b=1 /(110.8 \times 8.987)=1.004 \times 10^{-3} \operatorname{torr}^{-1}$
b) given that the total surface area of the charcoal is $13.9 \mathrm{~m}^{2}$, calculate the area occupied by each adsorbed molecule ( 5 pts )
Solution :
The surface area of the charcoal is given by
$\mathrm{SA}\left(\mathrm{m}^{2}\right)=\mathrm{V}_{\mathrm{m}}{ }^{0}(\mathrm{~L}) \times \mathrm{N}_{\mathrm{A}} \times a\left(\mathrm{~m}^{2}\right) / 22.4 \mathrm{~L}$
where $a$ is the area of 1 molecule
so
$a=\mathrm{SA}\left(\mathrm{m}^{2}\right) \times 22.4(\mathrm{~L}) /\left(\mathrm{V}_{\mathrm{m}}{ }^{\mathrm{o}}(\mathrm{L}) \times \mathrm{N}_{\mathrm{A}}\right)$
$=13.9 \mathrm{~m}^{2} \times 22.4 /\left(0.111 \times 6.02 \times 10^{23}\right)$
and $a=4.67 \times 10^{-21} \mathrm{~m}^{2}$ or $0.467 \AA^{2}$
c) what volume of CO would be adsorbed at 273 K when the pressure is 1 atm ? ( 5 pts )
(Use fitted isotherm)

Solution :
Knowing the parameter for the Langmuir eqn we just plug in the values

$$
\begin{aligned}
V & =\frac{V_{m} b P}{1+b P} \\
& =111 \mathrm{~mL} \times 1.00 \times 10^{-3} \text { torr }^{-1} \times 760 \text { torr } /\left(1+1.00 \times 10^{-3} \text { torr }^{-1} \times 760 \text { torr }\right)
\end{aligned}
$$

or
$V=47.9 \mathrm{~mL}$
3. (20 pts) Below are some data for the adsorption of $\mathrm{N}_{2}$ on 1.00 g of $\mathrm{TiO}_{2}$ at 75 K .

| p (torr) | 1.20 | 14.0 | 45.8 | 87.5 | 127.7 | 164.4 | 204.7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~V}\left(\mathrm{~mm}^{3}\right)$ | 601 | 720 | 822 | 935 | 1046 | 1146 | 1254 |

(Assume V corrected to 1 atm and 273 K )
For $\mathrm{N}_{2}$ at 75 K , take the vapor pressure $\mathrm{p}_{\mathrm{o}}=570$ torr
a) Rearrange the BET isotherm in the form $\mathrm{z} /\{(1-\mathrm{z}) \mathrm{V}\}=\ldots$. . where $\mathrm{z}=\left(\mathrm{p} / \mathrm{p}_{\mathrm{o}}\right)$. Find $\mathrm{V}_{\mathrm{m}}$ and c by a suitable plot on graph paper or spreadsheet/printer. (10 pts)
Solution :
The BET isotherm can be written :
$\frac{P}{V\left(P_{0}-P\right)}=\frac{1}{V_{m} c}+\frac{(c-1) P}{V_{m} c P_{0}}$
Setting $z=\left(\frac{P}{P_{0}}\right), \quad \frac{P}{V(1-z)}=\frac{1}{V_{m} c}+\frac{(c-1) z}{V_{m} c}$
So plotting the LHS vs. z gives
intercept $=\frac{1}{V_{m} c}$ and $\quad$ slope $=\frac{(c-1)}{V_{m} c}=\frac{1}{V_{m}}-\frac{1}{V_{m} c}=\frac{1}{V_{m}}-$ intercept
so $\quad V_{\mathrm{m}}=1 /($ slope + intercept $)$


| Po $=$ <br> $\mathbf{p}$ (Torr) | $\mathbf{V}$ (mm^3) | $\mathbf{z}=\mathbf{P} / \mathbf{P 0}$ | $\mathbf{z} /(\mathbf{1 - z ) \mathbf { V }}$ |
| ---: | ---: | :--- | :--- |
| 1.2 | 601 | $2.105 \mathrm{E}-03$ | $3.510 \mathrm{E}-06$ |
| 14 | 720 | $2.456 \mathrm{E}-02$ | $3.497 \mathrm{E}-05$ |
| 45.8 | 822 | $8.035 \mathrm{E}-02$ | $1.063 \mathrm{E}-04$ |
| 87.5 | 935 | $1.535 \mathrm{E}-01$ | $1.940 \mathrm{E}-04$ |
| 127.7 | 1046 | $2.240 \mathrm{E}-01$ | $2.760 \mathrm{E}-04$ |
| 164.4 | 1146 | $2.884 \mathrm{E}-01$ | $3.537 \mathrm{E}-04$ |
| 204.7 | 1254 | $3.591 \mathrm{E}-01$ | $4.469 \mathrm{E}-04$ |

Notice the poor SFs in the trend line, so let's do a full regression. The results are:

| Regression Statistics |  |
| :--- | ---: |
| Multiple R | 0.999829 |
| R Square | 0.999658 |
| Adjusted R Square | 0.99959 |
| Standard Error | $3.36 \mathrm{E}-06$ |
| Observations | 7 |

ANOVA

|  | $d f$ |  | $S S$ | $M S$ | $F$ | Significance $F$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Regression | 1 | $1.65 \mathrm{E}-07$ | $1.65 \mathrm{E}-07$ | 14633.14 | $7.32 \mathrm{E}-10$ |  |
| Residual | 5 | $5.63 \mathrm{E}-11$ | $1.13 \mathrm{E}-11$ |  |  |  |
| Total | 6 | $1.65 \mathrm{E}-07$ |  |  |  |  |


|  | CoefficientsStandard Error |  |  |  |  |  |  | $t$ Stat | $P$-value | Lower 95\% |
| :--- | :---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: |
| Intercept | $4.06 \mathrm{E}-06$ | $2.07 \mathrm{E}-06$ | 1.95772 | 0.107601 | $-1.3 \mathrm{E}-06$ |  |  |  |  |  |
| X Variable 1 | 0.001225 | $1.01 \mathrm{E}-05$ | 120.9675 | $7.32 \mathrm{E}-10$ | 0.001199 |  |  |  |  |  |

From the plot we find
$\mathrm{V}_{\mathrm{m}}=1 /($ slope + intercept $)=1 /\left(4.06 \times 10^{-6}+0.001225\right) \mathrm{mm}^{3}=814 \mathrm{~mm}^{3}$
and
$\mathrm{c}=1 /\left(\right.$ intercept $\left.\times \mathrm{V}_{\mathrm{m}}\right)=1 /\left(4.06 \times 10^{-6} \times 814\right)=303 \mathrm{~mm}^{-3}$
b) Assuming that the cross-sectional area of an $\mathrm{N}_{2}$ molecule in the liquid phase is $0.160 \mathrm{~nm}^{2}$, estimate the surface area of the sample in $\mathrm{m}^{2} / \mathrm{g}$. ( 5 pts )

Solution :

The surface area of the catalyst SA is given by
SA = \# surface sites $\times$ area per adsorbed molecule

$$
=\left[\mathrm{V}_{\mathrm{m}}{ }^{\mathrm{o}}(\mathrm{~L}) \times \mathrm{N}_{\mathrm{A}} / 22.4(\mathrm{~L})\right] \times a\left(\mathrm{~m}^{2}\right)
$$

and

$$
\begin{aligned}
\mathrm{SA} & =\left(0.814 \times 10^{-3} \mathrm{~L} \times 6.02 \times 10^{23} / 22.4 \mathrm{~L}\right) \times 0.160 \times 10^{-18} \mathrm{~m}^{2} \\
& =3.50 \mathrm{~m}^{2}
\end{aligned}
$$

