

**Worksheet #21**  
(Friday, December 1, 2023)

**Name**

**Question (5 pts):**

As you know, the uncertainty relation for arbitrary operators A, B is:

$$(\Delta A)^2 (\Delta B)^2 \geq \frac{1}{4} |\langle [A, B] \rangle|^2, \text{ where } \Delta A \text{ and } \Delta B \text{ are uncertainties. Derive the uncertainty}$$

relations for the case of  $A = X$  and  $B = P$  for 1D harmonic oscillator in a Hamiltonian eigenstate  $|n\rangle$ .

Comment on your result in the case of  $|n\rangle$  being the ground state (i.e.  $n=0$ ). Is this an expected result?